

Chapter 13 / **Example 11**

Using the inverse normal function

The inverse normal function uses either a left, right-tail or central areas. Care should be taken when calculating with this function to ensure the correct tail is being used.

For $X \sim N(21, 9)$

1 Find x given that:

a $P(X < x) = 0.8$

b $P(X > x) = 0.4$

2 a Find a and b given that $P(a < X < b) = 0.68$ and a and b are an equal distance either side of the mean.

b Verify that this supports the statement that approximately 68% of all data for a normally distributed population is likely to lie within one standard deviation of the mean.

Press **MENU** 2 **STAT** to display the List Editor screen.

Press **F5** DIST **F1** NORM **F3** InvN.

Select Data **F2** Var and Select Tail **F1** LEFT.

Enter the Area 0.8, 3 as the value of σ , 21 as the value of μ and leave the other items unchanged.

Use **▼** to navigate down to Execute and press **EXE**.

```
Inverse Normal
Data :Variable
Tail :Left
Area :0.8
σ :3
μ :21
Save Res:None
[None] LIST
```

$x = 23.5$.

```
Inverse Normal
xInv=23.5248637
```

Press **EXIT** to display the Inverse Normal template.

Select Tail **F2** RIGHT.

Enter the Area 0.4, leave 3 as the value of σ , 21 as the value of μ and the other items unchanged.

Use **▼** to navigate down to Execute and press **EXE**.

```
Inverse Normal
Data :Variable
Tail :Right
Area :0.4
σ :3
μ :21
Save Res:None
[None] LIST
```

$x = 21.8$.

```
Inverse Normal
xInv=21.7600413
```

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Press **EXIT** to display the Inverse Normal template.

Select Tail **F3** CENTRAL.

Enter the Area 0.68, leave 3 as the value of σ , 21 as the value of μ and the other items unchanged.

Use **▼** to navigate down to Execute and press **EXE**.

```

Inverse Normal
Data      :Variable
Tail      :Central
Area      :0.68
σ         :3
μ         :21
Save Res:None
[None] LIST
  
```

$a = 18.0$ and $b = 24.0$.

$18.0 = \mu - \sigma$, $24.0 = \mu + \sigma$.

```

Inverse Normal
x1 Inv=18.0166264
x2 Inv=23.9833736
  
```